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A generic fuel moisture content attenuation factor for fire spread rate empirical models

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Abstract

Aim of study: To develop a fuel moisture content (FMC) attenuation factor for empirical forest fire spread rate (ROS) models in general fire propagation conditions.

Methods: The development builds on the assumption that the main FMC-damping effect is a function of fuel ignition energy needs. *Main results:* The generic FMC attenuation factor was successfully used to derive ROS models from laboratory tests (n = 282) of fire spread in no-wind and no-slope, slope-, and wind-aided conditions. The ability to incorporate the FMC attenuation factor in existing field-based ROS models for shrubland fires and grassland wildfires (n = 123) was also positively assessed.

Research highlights: Establishing *a priori* the FMC-effect in field fires benefits the proper assessment of the remaining variables influence, which is normally eluded by heterogeneity in fuel bed properties and correlated fuel descriptors.

Additional keywords: fire behaviour; fire management; live and dead fuels; experimental fires; wildfires.

Symbols used: *a*, *b* (fitted coefficients); *c* (specific heat, kJ kg⁻¹ °C⁻¹; subscripts: f, fuel; w, water); $f_{\rm M}$ (fuel moisture content attenuation factor); *h* (fuel bed height, m); *M* (fine fuel moisture content, %; subscripts: d, dead fuels; l, live fuels); *Q* (heat per unit mass of fuel needs, kJ kg⁻¹; subscripts: i, fuel ignition; w, water evaporation); *R* (fire spread rate, m min⁻¹; subscripts: 0, no-wind and no-slope; S, slope-driven; U, wind-driven); *RH* (relative humidity, %); *S* (slope angle, °); *T* (temperature, °C; subscripts: a, air; f, fuel; i, ignition; v, vaporization); *U* (wind speed, km h⁻¹; subscript indicates measurement height, m); *w* (oven-dry fuel load, kg m⁻²); $\rho_{\rm b}$ (fuel bed density, kg m⁻³).

Authors' contributions: CGR conceived the theoretical approach, analysed the data, and wrote the paper.

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Introduction

Although many fire spread metrics can be analysed in the field of forest fire behaviour modelling, such as fuel time to ignition (Madrigal *et al.*, 2011), flame residence time (Burrows, 2001), and flame geometry (Nelson & Adkins, 1988), spread rate (R) prediction is the focus of most studies. R estimates can be useful to assist fire management activities, such as prescribed burning (Fernandes *et al.*, 2009) or wildfire suppression (Finney, 1998).

R models can be obtained via two distinct methods (Van Wagner, 1971): a physical approach, *i.e.*, a mathematical description of the processes behind fire spread (Linn *et al.*, 2002), or an empirical approach,

i.e., the development of relationships between fuel and environmental parameters, derived from laboratory (Rossa *et al.*, 2015a) or field fires (Fernandes *et al.*, 2000). Nevertheless, because of key limitations associated with physical models (Cruz *et al.*, 2017), such as complexity and high computation time, support to fire management operations is and will continue to be based on empirically-based predictions for the foreseeable future (Sullivan, 2009).

Typical empirical *R* formulations (Cruz *et al.*, 2015) account for the fuel moisture content (*M*) effect through an *M*-damping function, hereafter called fuel content attenuation factor ($f_{\rm M}$). Most frequently, $f_{\rm M}$ -functions are an exponential decay of the type exp(-*b M*) (Cheney *et al.*, 1993; Fernandes, 2001), but a power law of the type

a M^{-b} is sometimes used (Cheney *et al.*, 2012), where *a* and *b* are fitted coefficients. Both functional forms have advantages and shortcomings. Exponential decay f_M vary between 0 ($M = \infty$) and 1 (M = 0%) and allow obtaining a theoretical maximum *R*, *i.e.*, when fuel is moisture-free. However, because exponentials do not fit well to wide *M*-variations (Rossa & Fernandes, 2017a), extrapolations far outside the development *M*-range can be inaccurate. On the other hand, power law f_M provide a good fit to large *M*-intervals (Rossa, 2017), but do not offer reliable estimates for very low *M*-values because *R* tends rapidly to infinity when *M* approaches zero (Rossa & Fernandes, 2018a).

Although Rossa & Fernandes (2017a) show a very similar *M*-effect on *R* in no-wind and no-slope (R_0), slope-(R_s), and wind-driven (R_U) laboratory fires, currently, no f_M -function has been confirmed for the suitability to a general fire spread situation. In the present work, the hypothesis that a generic f_M can be used in empirical *R* models was tested. f_M was developed from the heat per unit mass of fuel requirements to ignite the fuel (Q_i) and does not have the above-mentioned constraints of exponential decay and power law functions. f_M was used to build *R* models from laboratory data and the ability to incorporate f_M in existing field-based models was also verified.

Methods

Fuel moisture content attenuation factor

Several factors beyond the heat needed to dry-out and ignite the fuel ahead of a flaming front have been attributed to the *M*-damping effect on *R* (Catchpole & Catchpole, 1991), such as the entrainment of moisture into the combustion zone and the attenuation of infrared radiation by water vapour released from unburnt fuel. Still, not discarding those effects, in the present work Q_i will be assumed as the main responsible for slowing down fire spread. Q_i is given by (Rossa & Fernandes, 2018b):

$$Q_{\rm i} = c_{\rm f} \left(T_{\rm i} - T_{\rm f} \right) + \frac{M}{100} \left[c_{\rm w} \left(T_{\rm v} - T_{\rm f} \right) + Q_{\rm w} \right]$$
[1]

where $c_{\rm f}$, $c_{\rm w}$, $T_{\rm i}$, $T_{\rm p}$, $T_{\rm v}$, and $Q_{\rm w}$, are, respectively, fuel specific heat, water specific heat, fuel igniting temperature, fuel initial temperature, water boiling temperature, and water latent heat of evaporation. In physically-based formulations (Thomas, 1971; Rothermel, 1972), $Q_{\rm i}$ is commonly used to account for the *M*-damping, as opposed to field-derived models. The relative *M*-effect on *R*, *i.e.*, $f_{\rm M}$, results from dry-towet fuel ignition needs ratio:

$$f_{\rm M} = \frac{\left(Q_{\rm i}\right)_{M=0}}{Q_{\rm i}}$$
^[2]

Although exponential decay or power law $f_{\rm M}$ functions used in field-based R models are generally based solely on M, they implicitly account for the main variables determining the energy requirements to achieve ignition, *i.e.*, T_{f} and M (Eq. [1]). But because T_{f} and Mare correlated for dead fuels, and dead fuels are present in most real-world fuel beds, specific f_M -factors work fine without explicitly accounting for T_{f} . This does not apply if $f_{\rm M}$ is based on $Q_{\rm H}$. As a result, defining the numerator of Eq. [2] requires establishing $T_{\rm f}$ for which M will become 0%. Otherwise, predicted $f_{\rm M}$ will be systematically above real $f_{\rm M}$ values, causing an over-prediction bias. I assumed that fuel will attain moisture-free conditions at $T_{e} = 100$ °C, which is water vaporization temperature and also roughly the temperature recommended to oven dry fuel samples (Matthews, 2010). If we consider the physical constants in Eq. [1] to be $c_f = 1.72 \text{ kJ kg}^{-1} \text{ °C}^{-1}$ (Balbi et *al.*, 2014), $c_{\rm w} = 4.19$ kJ kg⁻¹ °C⁻¹, $T_{\rm i} = 320$ °C, $T_{\rm v} = 100$ °C, and $Q_{\rm w}$ = 2260 kJ kg⁻¹ (Catchpole & Catchpole, 1991), we obtain:

$$f_{\rm M} = \frac{378.4}{1.72 \left(320 - T_{\rm f}\right) + \frac{M}{100} \left[4.19 \left(100 - T_{\rm f}\right) + 2260\right]}$$
[3]

Because it is not easy to measure or estimate $T_{\rm p}$ air temperature $(T_{\rm a})$ was used as a surrogate. $f_{\rm M}$ can theoretically vary between 0 and 1, as in the case of an exponential decay. Throughout the remainder of the paper $f_{\rm M}$ is Eq. [3], unless otherwise stated.

The M-effect on R will be restricted to fine fuels, which are responsible for 'carrying the fire' (Catchpole et al., 1993). M represents fuel bed overall water content and, hence, is obtained by weighing dead (M_d) and live (M_1) fuel moisture contents based on mass fractions in fuel beds composed of dead and live fuels (Rossa & Fernandes, 2017b). Usually, fuel bed M < 20% is achieved when vegetation is composed only of dead fuels, which respond to T_a variations. As M_d gets closer to zero, lowering its value requires an exponential T_a increase. On the other hand, fuel bed M > 20-30% is typically attained when vegetation also contains live fuels, whose M_1 is insensitive to $T_{\rm a}$. To obtain a continuous plot of $f_{\rm M}$ as a function of M, I considered an exponential T_{f} decrease between 100 °C for M = 0% and an arbitrary value of 15 °C for M = 20%, and constant $T_f = 15$ °C for M > 20%.

Laboratory data

A total of 282 laboratory fires were retrieved from several sources (Table 1). R_0 tests (n = 181) compiled in Rossa & Fernandes (2018a) include experiments from

| Data type | Model no. | Reference of data compilation | Fire spread type | Fuel bed | n | <i>w</i> (kg m ⁻²) | <i>h</i> (m) | T _a (°C) | М (%) | <i>R</i> (m min ⁻¹) |
|-------------------------------|--------------|-------------------------------------------------------|------------------------------------------------------|------------------------------------------------|-----|-----------------------------------|-----------------|------------------------|----------------|------------------------------------|
| Laboratory fires | 1 | Rossa & Fernandes (2018 <i>a</i>) ^A | No-wind and no-slope | Litter, slash, and shrub- like fuel beds | 181 | 0.45- 3.50 | 0.020- 0.508 | 13.0- 37.7 | 6.0- 161.7 | 0.025- 1.301 |
| | 2 | Rossa <i>et al.</i> (2016) | Slope-driven $(S = 20^{\circ})$ | Shrub-like fuel beds | 50 | 1.00- 1.74 | 0.500- 0.550 | 12.9- 26.8 | 12.9- 179.3 | 0.294- 2.000 |
| | 3 | Rossa & Fernandes (2017 <i>a</i>) | Wind-driven $(U = 8 \text{ km} \text{ h}^{-1})$ | Shrub-like fuel beds | 51 | 0.66- 2.43 | 0.292- 0.406 | 14.7- 26.8 | 18.0- 163.0 | 0.143- 1.285 |
| Field fires (experimental) | 4 | Anderson <i>et</i> $al. (2015)^{B}$ | Wind-driven $(U_2 = 2-25$ km h ⁻¹) | Shrublands | 100 | 0.32- 5.22 | 0.210- 4.800 | 7.0-33.0 | 26.8- 101.9 | 0.800- 43.90 |
| Wildfires | 5 | Cheney <i>et al.</i> (1998) ^C | Wind-driven $(U_{10} = 27-55 \text{ km h}^{-1})$ | Grasslands | 23 | - | - | 34.0- 43.0 | 2.6-4.2 | 66.67- 383.4 |

Table 1. Data sources and summary of fuel bed, ambient, and fire spread metrics.

Variables used were: *S*, slope angle; *U*, wind speed (subscript indicates measurement height); *w*, fuel load; *h*, fuel bed height; *T*_a, air temperature; *M*, fuel bed fine fuel moisture content (live and dead fuels); *R*, fire spread rate. ^AIncludes data from: Rossa (2009), Oliveira (2010) and Rossa & Fernandes (2018a). ^BIncludes data from: Catchpole (1987), Vega *et al.* (1998), Fernandes (2001), Vega *et al.* (2006), Anderson (2009), and Cruz *et al.* (2010). ^CIncludes data from: McArthur *et al.* (1982), Rawson *et al.* (1983), Keeves & Douglas (1983), Noble (1991), Maynes & Garvey (1985), McArthur (1966), Finocchiaro *et al.* (1970), Douglas (1970), and Cheney *et al.* (1998).

Rossa (2009) and Oliveira (2010), and pertain to fire spread in litter, slash, and shrub-like fuel beds, *i.e.*, vertically placed tree branches with or without a surface litter layer. Fuel beds were built using quasi-live, *i.e.*, collected live with *M* decreasing as a function of storage time, and dead vegetation of several species (*Pinus pinaster* Ait., *Eucalyptus globulus* Labill., *Eucalyptus obliqua* L'Her., *Acacia mangium* Willd., *Quercus robur* L., *Pinus resinosa* Sol. ex Ait.).

 $R_{\rm s}$ burns (n = 50) with slope angle (S) set to 20° were retrieved from Rossa *et al.* (2016). Fuel beds were made of vertically positioned quasi-live shrub and tree branches of four species: *Acacia dealbata* Link., *Cytisus striatus* (Hill) Rothm., *P. pinaster*, and *E. globulus*. In the *A. dealbata* tests, air-dried leaves had contracted folioles, because they fold inward when branches are cut from the plant and surface-to-volume ratio is greatly diminished, attaining a fire behaviour similar to the remaining fuel species.

The $R_{\rm U}$ experiments (n = 51) from Rossa & Fernandes (2017a) were carried out under constant wind speed (U) of 8 km h⁻¹ wind in shrub-like fuel beds, composed of vertically placed quasi-live tree branches over a dead litter layer. *P. resinosa* and *P. pinaster* needles were over-layered by *P. pinaster* branches, and *E. globulus* leaves were over-layered by *E. globulus* branches. In all laboratory trials (R_0 ,

 $R_{\rm s}, R_{\rm U}$), only the foliar fuel component was considered for computing oven-dry fuel bed load (*w*) and density ($\rho_{\rm L}$) in vegetation containing woody elements.

Experimental field fires and wildfires data

The applicability of $f_{\rm M}$ to real-world fire spread was tested based on 123 outdoors fires (experimental and wildfires). A comprehensive data set (n = 100), representative of global shrubland fire behaviour, was retrieved from Anderson *et al.* (2015), which compiled data from Catchpole (1987), Vega *et al.* (1998), Fernandes (2001), Vega *et al.* (2006), Anderson (2009), and Cruz *et al.* (2010).

Wildfires in fully cured grasslands (n = 23), compiled by Cheney *et al.* (1998), were used to test $f_{\rm M}$ for fire spread in very low *M* conditions, seldom attained in experimental fires. Data provenance was Cheney *et al.* (1998) own observations, McArthur (1966), Finocchiaro *et al.* (1970), Douglas (1970), McArthur *et al.* (1982), Rawson *et al.* (1983), Keeves & Douglas (1983), Maynes & Garvey (1985), and Noble (1991). Fuel beds were undisturbed, cut or grazed, and eatenout pastures. Because Cheney *et al.* (1998) did not report *M*, the Noble *et al.* (1980) equation describing the McArthur (1977) model: $M_{\rm d} = (97.7 + 4.06 RH)$ / ($T_{\rm a} + 6.0$) – 0.00854 *RH*, where *RH* is relative humidity, was used to obtain *M* estimates.

Data analysis and modelling

 $f_{\rm M}$ was used to develop R_0 , $R_{\rm s}$, and $R_{\rm U}$ models from the laboratory fire spread data. In the Rossa & Fernandes (2018a) R_0 formulation based on fuel bed height (*h*) and *M*, the *h*-exponent is close to unity. So, for the sake of simplicity, a linear *h*-effect was assumed. The present R_0 model was obtained by linear fitting R_0 to $h f_{\rm M}$. In the case of $R_{\rm s}$ and $R_{\rm U}$ data, structural fuel bed metrics of most trials were close to the experimental mean, despite some variation between observed minimum and maximum *h* and *w* values. Also, both *S* and *U* were kept constant. As a result, *M* was the parameter with most influence on $R_{\rm s}$ and $R_{\rm U}$, and both models were obtained by establishing a linear relationship between *R* and $f_{\rm M}$.

Both studies where field fires were compiled (Cheney *et al.*, 1998; Anderson *et al.*, 2015) provide *R* models accounting for the *M*-effect through an exponential decay $f_{\rm M}$, which, like Eq. [3] $f_{\rm M}$, varies in the 0–1 range. Thus, the concept of using a generic $f_{\rm M}$ -function was tested by using the original *R* models, substituting their original (specific) $f_{\rm M}$ by the proposed generic $f_{\rm M}$. In mixed live and dead fuel complexes, this exchange can only be done if the specific $f_{\rm M}$ -function accounts for both $M_{\rm d}$ and $M_{\rm l}$, as in Anderson *et al.* (2015). Specific $f_{\rm M}$ were plotted against generic $f_{\rm M}$ -values and predictions using both $f_{\rm M}$ -functions were evaluated for comparison.

Goodness of fit of linear regressions was assessed based on the coefficient of determination (R^2). All predictions (laboratory and field fires) were evaluated using deviation measures: root mean square error (RMSE), mean absolute error (MAE), mean absolute percentage error (MAPE), and mean bias error (MBE) (Willmott, 1982).

Results

Both in the laboratory (6.0–179.3%) and outdoors (2.6–101.9%) fires the *M*-range was very wide (Table 1). Wildfires allowed testing $f_{\rm M}$ for extreme fire spread conditions with U_{10} (measured at a 10-m height) up to 55 km h⁻¹ and an impressive *R* of 383.4 m min⁻¹ (23 km h⁻¹). As expected, $f_{\rm M}$ evolution with *M* (Fig. 1) resembles the *M*-damping plots obtained using power law $f_{\rm M}$ -functions (Rossa, 2017), which are able to describe the *M*-effect well over wide ranges.

All laboratory *R* relationships yielded a good fit to the data (Fig. 2) with R^2 between 0.651 and 0.9. Model evaluation (Table 2) confirms these figures, with MAE and MAPE, respectively, in the range 0.06–0.19 m min⁻¹ and 16.2–28.9%. $f_{\rm M}$ testing with field fires showed highly significant correlations (*p*<0.0001) between specific

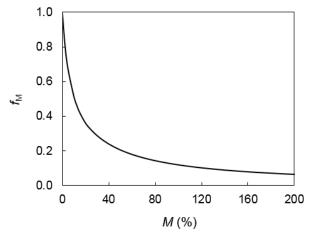


Figure 1. Fuel moisture content attenuation factor (f_M , Eq. [3]) as a function of fuel bed moisture content (M). f_M was computed considering an exponential fuel temperature (T_f) decrease between 100 °C for M = 0% and 15 °C for M = 20%; $T_f = 15$ °C was assumed for M > 20%. See the 'Methods' section for details.

and generic $f_{\rm M}$ -derived values (Fig. 3), respectively of 0.457 for shrubland and 0.995 for grassland fires. The lower correlation for shrubland suggests a diminished sensitivity of the generic $f_{\rm M}$ to M. Nevertheless, generic $f_{\rm M}$ produced accurate predictions of all field data (Fig. 4) and, in fact, allowed for an overall improvement in model performance, for example with a decrease in MAPE from 70.6 to 63.4% in shrubland fires and 26.7 to 24.8% in grassland wildfires. Of course, the quality of predictions is mostly dictated by the original R formulation and these results only demonstrate that the proposed generic $f_{\rm M}$ is a reasonable surrogate for the specific $f_{\rm M}$.

Discussion

$f_{\rm M}$ performance and applicability

Laboratory-based R models built with the generic $f_{\rm M}$ showed good agreement with data. They yielded R^2 slightly below those obtained using the original power law $f_{\rm M}$ -based models (0.667–0.947), but significantly above the 0.566 and 0.665 values obtained for the $R_{\rm s}$ and $R_{\rm U}$ models using exponentials (Rossa *et al.*, 2016; Rossa & Fernandes, 2017a, 2018a). Despite a small decrease in accuracy, when compared with the use of power laws, the generic $f_{\rm M}$ provides important benefits, such as not becoming extremely sensible at very low M-values and allowing extrapolation to moisture-free conditions. The generic $f_{\rm M}$ allowed improved prediction ability in relation to the specific $f_{\rm M}$ -functions used in existing field-based models for shrubland experimental fires and grassland wildfires.

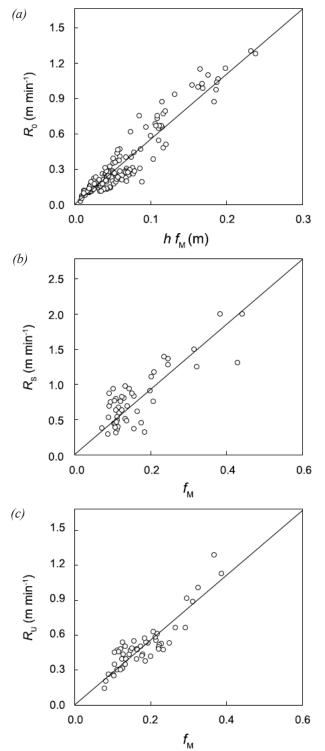


Figure 2. Laboratory-derived fire spread rate (*R*) models based on fuel moisture content attenuation factor (f_M , Eq. [3]) for: (*a*) no-wind and no-slope spread (R_0) in litter, slash, and shrub-like fuel beds, *h* is fuel bed height, linear fit is model 1 in Table 2 ($R^2 = 0.900$); (*b*) slope-driven spread (R_s) in shrub-like fuel beds, linear fit is model 2 in Table 2 ($R^2 = 0.651$); and (*c*) wind-driven spread (R_U) in shrub-like fuel beds, linear fit are the fuel beds, linear fit is model 2 ($R^2 = 0.795$). All regressions were significant at p < 0.0001. See Table 1 for data sources.

Laboratory data included a great number of tests in several fire spread conditions over a wide *M*-range, and fuel beds were very diverse in terms of species and structure. R_0 laboratory tests are representative of field R_0 and a reasonable surrogate for backing fires R (Rossa, 2017; Rossa & Fernandes, 2018a). That is not the case of slope and wind-driven laboratory trials, in which *R* is limited by the fire front width (Fernandes *et al.*, 2009). Shrubland and grassland outdoors fires enabled the positive testing of $f_{\rm M}$ in $R_{\rm U}$ conditions free of scaling issues. There is no apparent reason for $f_{\rm M}$ not to hold for slope-driven field fires as well. Not excluding the need of further assessing $f_{\rm M}$ with additional field data, its overall performance in all tested fire spread situations lends strong support to its ability of successfully incorporating empirically-based R models in generic fire spread conditions.

If Eq. [3] were developed without assuming that moisture-free conditions will be attained at $T_{f} = 100$ °C, *i.e.*, with the numerator becoming 1.72 $(320 - T_f)$ instead of 378.4, using the generic $f_{\rm M}$ in the fieldderived R models would yield MBE of 3.92 and 41.7 m min⁻¹, respectively for shrubland and grassland fires. The arising of this substantial over-prediction bias lends support to the supposition that $f_{\rm M}$ -functions based only on M implicitly account for T_{f} . In other words, this means that in a hypothetical situation of fire spread through a dry fuel bed at, for example, $T_f = 20$ °C, predicted R using typical empirical field-based models would be higher than observed because the M-functions were fitted in conditions where the decrease in M is concurrent with increasing $T_{\rm f}$. As a result, estimated $f_{\rm M}$ attains its maximum, *i.e.*, fire spread attenuation is minimum, although fuel conditions will delay fuel ignition more than expected in an extrapolation to M = 0%, where $T_{\rm f}$ was supposed to grow concomitantly with diminishing M. It is important to notice that this rationale was derived from results using a limited field data set, hence further testing with additional data would benefit its confirmation.

Advantages and limitations

 $M_{\rm d}$ of field fuels is easy to sample. Overall M determination requires measuring both $M_{\rm d}$ and $M_{\rm l}$ (Rossa *et al.*, 2015b), as well as assessing dead and live fuel mass fractions, which may be problematic in very heterogeneous fuel complexes. This is a limitation of using the generic $f_{\rm M}$, when compared to $f_{\rm M}$ -functions accounting for only the $M_{\rm d}$ -effect. Most empirical fuel-dependent models rely on the sole use of $M_{\rm d}$ (Cruz *et al.*, 2015) to provide a satisfactory R explanation, which restricted the data available to test the specific $f_{\rm M}$ -function proposed in the present work. Field-based

| le 2. Model evaluation metrics (see Table 1 for details on fire spread data). | | | | | | | |
|-------------------------------------------------------------------------------|------------|--------------------------------|-------------------------------|--|--|--|--|
| Model | $f_{ m M}$ | RMSE (m min ⁻¹) | MAE (m min ⁻¹) | | | | |
| $R_0 = 5.53 \ h f_{\rm M}$ | Eq. [3] | 0.0864 | 0.0624 | | | | |

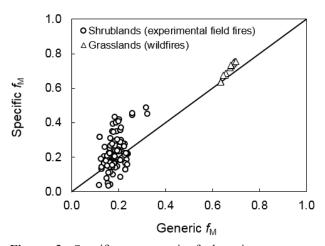
Tabl

| Model | $f_{ m M}$ | RMSE (m min ⁻¹) | MAE (m min ⁻¹) | MAPE (%) | MBE (m min ⁻¹) |
|------------------------------------------------------------|---------------------------------------|--------------------------------|-------------------------------|-------------|-------------------------------|
| (1) $R_0 = 5.53 h f_M$ | Eq. [3] | 0.0864 | 0.0624 | 23.7 | 0.0044 |
| (2) $R_{\rm s} = 4.63 f_{\rm M}$ | Eq. [3] | 0.2352 | 0.1891 | 28.9 | -0.0340 |
| (3) $R_{\rm U} = 2.79 f_{\rm M}$ | Eq. [3] | 0.0966 | 0.0773 | 16.2 | -0.0036 |
| (4) $R_{\rm U} = 6.42 \ U_2^{0.994} \ h^{0.372} f_{\rm M}$ | $\exp(-0.0761 M_{d} - 0.00313 M_{l})$ | 6.3070 | 4.5524 | 70.6 | 1.3627 |
| | Eq. [3] | 6.2379 | 4.5075 | 63.4 | -0.3927 |
| (5) $R_{\rm U} = (a + b (U_{10} - 5))^{0.844} f_{\rm M}$ | $exp(-0.108 M_{d})$ | 56.483 | 43.964 | 26.7 | 0.9197 |
| | Eq. [3] | 58.824 | 43.955 | 24.8 | -6.534 |

Variables used were: $f_{\rm M}$, fuel moisture content attenuation factor; R, fire spread rate (subscripts indicate: 0, no-wind & no-slope; S, slope-driven; U, wind-driven); h, fuel bed height; U, wind speed (subscript indicates measurement height); M, fine fuel moisture content (subscripts indicate: d, dead fuels; l, live fuels); a, b, fitted coefficients dependant on grassland type (Cheney et al., 1998). Models 4 and 5 were evaluated using their original $f_{\rm M}$ and the one proposed in Eq. [3].

models based only on $M_{\rm d}$ work well because, usually, M_1 is either constant or correlated with M_d for a given fuel complex (Rossa & Fernandes, 2017b).

Nevertheless, especially for experimental programs composed of a limited number of tests, possible difficulties in assessing overall M might pay-off in terms of the advantages of using a generic $f_{\rm M}$. The use of experimental outdoors fires as a source of development data is appealing because of the strong resemblance to real-world fire-spread. However, this option is often challenged by heterogeneity in fuel bed properties and correlated fuel descriptors, which elude the correct quantification of specific effects (Rossa & Fernandes, 2017b). Establishing a priori the M-effect through the use of $f_{\rm M}$ significantly simplifies the proper assessment of the remaining influent variables.



Conclusion

A generic $f_{\rm M}$ -function for empirical R models was developed based on the assumption that the main *M*-damping effect is a function of Q_i . f_M was successfully used to derive R models from laboratory

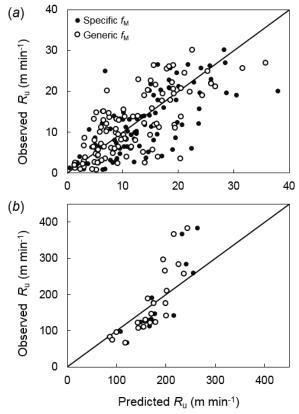


Figure 3. Specific vs. generic fuel moisture content attenuation factor (f_{M}) for shrubland fires and grassland wildfires. Specific $f_{\rm M}$ are given in Table 2; generic $f_{\rm M}$ is Eq. [3]. Solid line is perfect agreement; correlation between variables is 0.457 for shrubland fires and 0.995 for grassland wildfires (p < 0.0001). See Table 1 for data sources.

Figure 4. Observed vs. predicted wind-driven fire spread rate (R_{II}) using the specific fuel moisture content attenuation factor (f_{M}) (Table 2) and the generic f_{M} (Eq. [3]) for: (a) shrubland fires; and (b) grassland wildfires. Solid lines are perfect agreement. See Table 1 for data sources.

fire spread in no-wind and no-slope, slope-, and wind-aided conditions. The ability to incorporate $f_{\rm M}$ in existing field-based models was also positively assessed. Possible difficulties in assessing overall M due to fuel complex heterogeneities, might pay-off in terms of the advantages of using a tested generic $f_{\rm M}$. For example, establishing *a priori* the *M*-effect benefits the proper quantification of the remaining variables influence. Not excluding the need of further assessing $f_{\rm M}$ with additional field data, its overall performance in all tested fire spread situations lends strong support to its ability of successfully incorporating empirically-based *R* models in generic fire spread conditions.

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References

- Anderson SA, 2009. Future options for fire behaviour modelling and fire danger rating in New Zealand. Proc Roy Soc Queensland 115: 119-127.
- Anderson WR, Cruz MG, Fernandes PM, McCaw L, Vega JA, Bradstock R, Fogarty L, Gould J, McCarthy G, Marsden-Smedley JB, *et al.*, 2015. A generic, empirical-based model for predicting rate of fire spread in shrublands. Int J Wildl Fire 24 (4): 443-460. https://doi.org/10.1071/WF14130
- Balbi JH, Viegas DX, Rossi JL, Rossa CG, Chatelon FJ, Cancellieri D, Simeoni A, Marcelli T, 2014. Surface fires: no wind, no slope, marginal burning. J Environ Sci Eng A: 73-86.
- Burrows ND, 2001. Flame residence times and rates of weight loss of eucalypt forest fuel particles. Int J Wildl Fire 10 (2): 137-143. https://doi.org/10.1071/WF01005
- Catchpole WR, 1987. Heathland fuel and fire modelling. PhD thesis, Australian Defence Force Academy, University of New South Wales, Canberra, ACT, Australia.
- Catchpole EA, Catchpole WR, 1991. Modelling moisture damping for fire spread in a mixture of live and dead fuels. Int J Wildl Fire 1 (2): 101-106. https://doi.org/10.1071/ WF9910101
- Catchpole EA, Catchpole WR, Rothermel RC, 1993. Fire behavior experiments in mixed fuel complexes. Int J Wildl Fire 3 (1): 45-57. https://doi.org/10.1071/WF9930045
- Cheney NP, Gould JS, Catchpole WR, 1993. The influence of fuel, weather and fire shape variables on fire-spread in grasslands. Int J Wildl Fire 3 (1): 31-44. https://doi. org/10.1071/WF9930031

- Cheney NP, Gould JS, Catchpole WR, 1998. Prediction of fire spread in grasslands. Int J Wildl Fire 8 (1): 1-13. https:// doi.org/10.1071/WF9980001
- Cheney NP, Gould JS, McCaw WL, Anderson WR, 2012. Predicting fire behaviour in dry eucalypt forest in southern Australia. For Ecol Manag 280: 120-131.
- Cruz MG, Matthews S, Gould J, Ellis P, Henderson M, Knight I, Watters J, 2010. Fire dynamics in mallee-heath: fuel, weather and fire behaviour prediction in South Australian semi-arid shrublands. Bushfire Cooperative Research Centre Report A.10.01, Melbourne, Victoria, Australia.
- Cruz MG, Gould JS, Alexander ME, Sullivan AL, McCaw WL, Matthews S, 2015. Empirical-based models for predicting head-fire rate of spread in Australian fuel types. Aust Forestry 78 (3): 118-158. https://doi.org/10.1080/00 049158.2015.1055063
- Cruz MG, Alexander ME, Sullivan AL, 2017. Mantras of wildland fire behaviour modelling: facts or fallacies? Int J Wildl Fire 26 (11): 973-981. https://doi.org/10.1071/ WF17097
- Douglas DR, 1970. Wind changes and your tactics. EFS Manual. pp: 7-10.
- Fernandes PM, 2001. Fire spread prediction in shrub fuels in Portugal. For Ecol Manag 144 (1): 67-74.
- Fernandes PM, Catchpole WR, Rego FC, 2000. Shrubland fire behaviour modelling with microplot data. Can J For Res 30 (6): 889-899. https://doi.org/10.1139/x00-012
- Fernandes PM, Botelho HS, Rego FC, Loureiro C, 2009. Empirical modelling of surface fire behaviour in maritime pine stands. Int J Wildl Fire 18 (6): 698-710. https://doi. org/10.1071/WF08023
- Finney MA, 1998. FARSITE: fire area simulator Model development and valuation. USDA Forest Service Research Paper RMRS-RP-4.
- Finocchiaro N, Lindforth DJ, Shields BT, 1970. Report on the meteorological aspects of the extensive grassfires in Victoria on 8 January 1969. Commonwealth Bureau of Meteorology, Working Paper No. 127, Melbourne, Australia.
- Keeves A, Douglas DR, 1983. Forest fires in South Australia on 16 February 1983 and consequent future forest management aims. Aust Forest 46 (3): 148-162. https:// doi.org/10.1080/00049158.1983.10674394
- Linn R, Reisner J, Colman JJ, Winterkamp J, 2002. Studying wildfire behavior using FIRETEC. Int J Wildl Fire 11 (4): 233-246. https://doi.org/10.1071/WF02007
- Madrigal J, Guijarro M, Hernando C, Díez C, Marino E, 2011. Effective heat of combustion for flaming combustion of Mediterranean forest fuels. Fire Technol 47 (2): 461-474. https://doi.org/10.1007/s10694-010-0165-x
- Matthews S, 2010. Effect of drying temperature on fuel moisture content measurements. Int J Wildl Fire 19 (6): 800-802. https://doi.org/10.1071/WF08188

- Maynes KJ, Garvey MF, 1985. Report on selected major fires in country areas of Victoria on 14th January, 1985. Country Fire Authority of Victoria, Melbourne, Australia.
- McArthur AG, 1966. Weather and grassland fire behaviour. Dept. of Nat. Devel., Forestry and Timber Bureau, Canberra, Australia. Leaflet 100.
- McArthur AG, 1977. Grassland Fire Danger Meter Mk V, linear slide-rule. Country Fire Authority of Victoria, Melbourne.
- McArthur AG, Cheney NP, Barber J, 1982. The fires of 12 February 1977 in the Western District of Victoria. CSIRO Division of Forestry Research, Canberra and Country Fire Authority of Victoria, Melbourne, Australia.
- Nelson RM, Adkins CW, 1988. A dimensionless correlation for the spread of wind-driven fires. Can J For Res 18 (4): 391-397. https://doi.org/10.1139/x88-058
- Noble JC, 1991. Behaviour of a very fast grassland wildfire on the Riverine Plain of south-eastern Australia. Int J Wildl Fire 1 (3): 189-196. https://doi.org/10.1071/WF9910189
- Noble IR, Bary GA, Gill AM, 1980. McArthur's fire-danger meters expressed as equations. Aust J Ecol 5 (2): 201-203. https://doi.org/10.1111/j.1442-9993.1980.tb01243.x
- Oliveira RF, 2010. Um estudo sobre os incêndios florestais ocorridos no Estado de Vitória (Austrália), em Fevereiro de 2009. MSc thesis, University of Coimbra, Portugal.
- Rawson RP, Billing PR, Duncan SF, 1983. The 1982-83 forest fires in Victoria. Aust Forest 46 (3): 163-172. https://doi.or g/10.1080/00049158.1983.10674395
- Rossa CG, 2009. Dynamic model for fire behaviour prediction. PhD thesis, University of Coimbra, Portugal.
- Rossa CG, 2017. The effect of fuel moisture content on the spread rate of forest fires in the absence of wind or slope. Int J Wildl Fire 26 (1): 24-31. https://doi.org/10.1071/ WF16049
- Rossa CG, Fernandes PM, 2017a. Fuel-related fire behaviour relationships for mixed live and dead fuels burned in the laboratory. Can J For Res 47 (7): 883-889. https://doi.org/10.1139/cjfr-2016-0457
- Rossa CG, Fernandes PM, 2017b. Short communication: On the effect of live fuel moisture content on fire rate of spread. For Syst 26 (3): eSC08.
- Rossa CG, Fernandes PM, 2018a. Empirical modelling of fire spread rate in no-wind and no-slope conditions. Forest Sci: fxy002. https://doi.org/10.1093/forsci/fxy002

- Rossa CG, Fernandes PM, 2018b. On the fire-spread rate influence of some fuel bed parameters derived from Rothermel's model thermal energy balance. Sumar List 142 (1-2): 77-80. https://hrcak.srce.hr/194637
- Rossa CG, Davim DA, Viegas DX, 2015a. Behaviour of slope and wind backing fires. Int J Wildl Fire 24 (8): 1085-1097. https://doi.org/10.1071/WF14215
- Rossa CG, Fernandes PM, Pinto A, 2015b. Measuring foliar moisture content with a moisture analyzer. Can J For Res 45 (6): 776-781. https://doi.org/10.1139/cjfr-2014-0545
- Rossa CG, Veloso R, Fernandes PM, 2016. A laboratorybased quantification of the effect of live fuel moisture content on fire spread rate. Int J Wildl Fire 25 (5): 569-573. https://doi.org/10.1071/WF15114
- Rothermel RC, 1972. A mathematical model for predicting fire spread in wildland fuels. USDA Forest Service Intermountain Forest and Range Experiment Station. Ogden, Utah. Research Paper INT-115.
- Sullivan AL, 2009. Wildland surface fire spread modelling; 1990-2007. 1: Physical and quasi-physical models. Int J Wildl Fire 18 (4): 349-368. https://doi.org/10.1071/ WF06143
- Thomas PH, 1971. Rates of spread of some wind-driven fires. Forest 44: 155-175. https://doi.org/10.1093/forest-ry/44.2.155
- Van Wagner CE, 1971. Two solitudes in forest fire research. Canadian Forest Service, Petawawa Forest Experiment Station. Chalk River, Ontario. Information Report PS-X-29.
- Vega JA, Cuinas P, Fonturbel T, Perez-Gorostiaga P, Fernandez C, 1998. Predicting fire behaviour in Galician (NW Spain) shrubland fuel complexes. Proc III Int Conf on Forest Fire Research, and 14th Conf on Fire and Forest Meteorology, Luso, Portugal, 16–20 November; Viegas DX, ed) Vol. II, pp: 713-728. University of Coimbra, Portugal.
- Vega JA, Fernandes P, Cuinas P, Fonturbel MT, Loureiro C, 2006. Fire spread analysis of early summer field experiments in shrubland fuel types of northwestern Iberia. For Ecol Manag 234 (S): S102.
- Willmott CJ, 1982. Some comments on the evaluation of model performance. Bull Am Meteorol Soc 63 (11): 1309-1313. https://doi.org/10.1175/1520-0477(1982)063<1309:SCO TEO>2.0.CO;2